Intertemporal Consumption and Debt Aversion: An Experimental Study

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Abstract

This paper tests how subjects behave in an intertemporal consumption/saving experiment when borrowing is allowed and whether subjects treat debt differently than savings. Two treatments create environments where either saving or borrowing is required for optimal consumption. Since both treatments share the same optimal consumption levels, observed consumption choices can be directly compared across treatments. The experimental findings imply that deviations from optimal behavior are higher when subjects have to borrow than when they have to save in order to consume optimally, suggesting debt aversion. Significant under-consumption is observed when subjects have to borrow in order to reach optimal consumption. In line with previous experiments, weak evidence is found suggesting that subjects over-consume when saving is necessary for optimal consumption.

**JEL-Classification:** C91, D91, E21

**Keywords:** Laboratory Experiment, Intertemporal Consumption, Consumption Smoothing, Debt Aversion

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1 Introduction

The question how people cope with stochastic dynamic optimization problems, such as posed by intertemporal consumption/savings problems, has been repeatedly tested in economic experiments. The main finding of this literature is that subjects (somewhat unsurprisingly) deviate systematically from optimal behavior. In particular it is observed that subjects tend to over-consume in early periods, i.e. save too little compared to the optimal solution, and that consumption tracks income too closely. When subjects are given the opportunity to learn (either privately through repetition or socially through observing other life-cycle consumption decisions) consumption decisions improve towards optimality.

With the exception of fenig2013 however, all existing experimental studies on dynamic intertemporal consumption/savings problems have strict borrowing constraints. This implies that only one side of the problem has been examined, i.e. whether subjects save optimally. I believe that the question whether individuals borrow optimally is of similar interest to the understanding of intertemporal consumption decisions. This is because borrowing is as much a means to smoothing consumption (i.e. consuming optimally) as is saving. Therefore, sub-optimal borrowing decisions affect welfare in the same detrimental way as sub-optimal saving decisions.

The aim of this paper is to address two main research questions: first, how do people behave in a life-cycle consumption experiment when borrowing is allowed and necessary for optimal consumption? Second, do people treat savings systematically different than debt with respect to consumption smoothing?

The experiment conducted for this paper is based on a simple discrete-time, finite horizon life-cycle model of consumption with no discounting and no interest paid on savings or debt. In order to compare borrowing and saving behavior this experiment has two treatments, one in which the income stream has an increasing trend and one in which it has a decreasing trend. Since the experimental environment creates an incentive to smooth consumption, the optimal solution with an increasing income stream requires borrowing and the optimal solution with a decreasing income stream requires

\footnote{An early reference is hey1988 noussair2000 lei2002 ballinger2011 carbone2004 carbone2006 brown2009 as well as carbone2013 further substantiate the experimental analysis of intertemporal consumption/saving problems.}

\footnote{See duffy2012 for an excellent survey of intertemporal consumption/savings experiments.}

\footnote{The experiment by fenig2013 has treatments without borrowing constraints. They find that prohibiting borrowing for speculation in an experimental general equilibrium economy leads to increased precautionary saving and smaller asset price bubbles.}
saving. Moreover, since the specifics of the underlying model were chosen in such a way that optimal consumption is the same in both treatments, this allows to directly compare borrowing and saving behavior. This is a novel feature compared to previous experimental work where mostly stationary income processes are used, which does not allow for such a comparison.\footnote{\cite{brown2009} use an income stream that is increasing in expectations. However, their experiment also uses habit formation utility and therefore saving is optimal in early periods even with an increasing income stream.}

With an increasing income stream, the experimental data suggests that subjects significantly underconsume, that is they do not borrow enough compared to the optimal solution. This stands in contrast to evidence from previous experiments on intertemporal consumption/savings problems, where overconsumption is typically observed. In line with previous findings, however, weak evidence is found for overconsumption in the treatment with a decreasing income stream, implying that subjects do not save enough relative to the optimal solution. Comparing consumption decisions across treatments reveals that deviations from optimal behavior are higher in the treatment with an increasing income stream compared to the treatment with a decreasing income stream. This implies that subjects are less willing to borrow than they are willing to save in order to smooth consumption, i.e. they are debt averse. To my knowledge, this paper is the first to provide clear evidence for this asymmetry between borrowing and saving behavior in an intertemporal consumption/saving experiment.

The experimental literature on intertemporal consumption/savings problems concentrates on two potential explanations for suboptimal behavior. One explanation is bounded rationality or cognitive constraints. \cite{ballinger2011} for example find that cognitive ability is the best predictor of saving performance. Moreover there exists substantial evidence that subjects typically learn to improve their consumption decisions over time. This points towards bounded rationality since with perfect rationality there would be no room for improvement. In the experiment conducted for this paper, cognitive constraints certainly explain some deviations from optimal behavior. However they cannot explain systematic differences in deviations from optimal behavior in the two treatments of this experiment, since the experimental task is equally demanding in both treatments. This is because subjects face essentially the same optimization problem in both treatments, as debt is mathematically equivalent to savings only with a different sign.

Another explanation for suboptimal behavior is a preference for immediacy or
present bias. brown2009 use immediate rewards in an intertemporal consumption/saving experiment. They find that behavior is consistent with both hyperbolic discounting and dual self models and not with exponential discounting. In this experiment, however, present bias should not play a role since subjects receive their reward at only one point in time – at the end of the experiment.

The existing literature on debt aversion primarily analyzes its role in the light of the decision to invest in higher education. eckel2007 use survey measures to assess debt aversion and relate this data to lottery choice experiments. They find that debt aversion has little to no impact on the demand for loans for postsecondary education. In field experiments, field2009 as well as caetano2011 offer differently labeled loan contracts to students and find that debt aversion does influence career and education investment decisions. However, all these studies analyze debt aversion in the context of student loans. This experiment offers a different approach, allowing to identify debt aversion in the context of a stochastic dynamic optimization problem, which in one way or another serves as a basis for household behavior in most modern macroeconomic models.

The remainder of the paper is organized as follows. The next section provides the theory and experimental design. Section 3 contains the data analysis and Section 4 concludes.

2 Theory and Experimental Design

The experiment described in the following section aims to implement a particular version of the life-cycle model of consumption. One experimental life-cycle lasts for $T = 20$ periods. In each period $t = (1, ..., 20)$, subjects decide how much to consume ($c_t$), and implicitly how much to save or borrow. There is no discounting and no interest is paid on savings or debt. Period income $y_t$ follows a trend stationary stochastic process. The intertemporal budget constraint requires period consumption plus period savings ($a_t$) to equal period wealth, which is defined as $w_t = y_t + a_{t-1}$. Period savings are allowed to be both positive and negative. In the last period, remaining wealth must be consumed, i.e. saving for the (non-existent) next period is not possible. Initial savings $a_0$ were normalized to zero.\textsuperscript{5} Induced preferences are given by a time-separable CARA utility function: $u(c_t) = 250(1 - e^{-\theta c_t})$, where the coefficient of absolute risk aversion $\theta$ is set

\textsuperscript{5}Note that together with the ending condition ($a_{20} = 0$), this also implies that total consumption must equal total income: $\sum_{t=1}^{20} c_t = \sum_{t=1}^{20} y_t$. 

4
to 0.02. The subjects’ objective was to choose consumption in every period in order to maximize the expected utility of life-time consumption. The decision problem subjects face at any period $\tau$ can be written as:

$$\max_{c_t} E_{\tau} \sum_{t=\tau}^{T} u(c_t)$$  \hspace{1cm} (1)$$

s.t. $c_t + a_t = w_t,$  \hspace{1cm} (2)

$a_0 = 0,$  $a_T = 0.$ \hspace{1cm} (3)

caballero1991 shows that with CARA utility, this optimization problem has a closed-form analytic solution. For any income process $y_t = y_0 + st + \varepsilon_t,$ where $P(\varepsilon_t = \sigma_\varepsilon) = P(\varepsilon_t = -\sigma_\varepsilon) = 1/2, \forall t,$ optimal consumption at time $t$ is equal to:7

$$c^*_t(w_t) = \frac{1}{T-t+1} \left[ w_t + \xi_t - \Gamma_t(\theta \sigma_\varepsilon) \right].$$ \hspace{1cm} (4)$$

$$\xi_t = (T-t) \left( y_0 + s \left( \frac{T + t + 1}{2} \right) \right).$$ \hspace{1cm} (5)$$

$$\Gamma_t(\theta \sigma_\varepsilon) = \sum_{j=0}^{T-t} \sum_{i=1}^{j} \log \cosh \left( \frac{\theta \sigma_\varepsilon}{T-t+1-i} \right).$$ \hspace{1cm} (6)$$

Optimal period consumption is linear in period wealth. The sum of future expected income is denoted by $\xi_t = E_t \left[ \sum_{j=1}^{T-t} y_{t+j} \right].$ Precautionary saving, $\Gamma_t(\theta \sigma_\varepsilon),$ depends on the parameter of absolute risk aversion and the standard deviation of the income process ($\sigma_\varepsilon$).

The experiment has two base treatments that differ only with respect to the income process. In one treatment the income process is increasing over time, in the other one it is decreasing. Intuitively, the optimal solution with an increasing income process includes borrowing whereas with a decreasing income process saving is necessary for optimal consumption. Therefore I will refer to the treatment with the increasing income stream as the Borrowing treatment and to the treatment with a decreasing income process...
stream as the Saving treatment. The income process for the Borrowing treatment is given by: \( y_B^t = 10t + \varepsilon_t \), where \( \varepsilon_t \) takes the values of +10 or -10, each with probability of one half. For the Saving treatment the income process is: \( y_S^t = 210 - 10t + \varepsilon_t \). Note that the expected lifetime income over 20 periods is equal across treatments. Since the stochastic component is equivalent at any time for both treatments and income can be shifted costlessly across periods, this implies that optimal consumption plans are equivalent in both treatments. The experimental design therefore allows to directly compare consumption behavior in both treatments (between subject) and thus to examine whether there exist systematic differences between saving and borrowing behavior.

In order to assess learning effects, the experiment is repeated for six experimental life cycles (rounds), with different income realizations in each round. Subjects first play three repetitions of either the Borrowing or the Saving treatment. After three repetitions roles are changed. Subjects who started with the Borrowing treatment now play three repetitions of the Saving treatment and vice versa.\(^8\) This role change was implemented in order to analyze whether subjects are able to transfer their learning from one treatment to the other. Moreover, this adds a within subject dimension to the analysis of the treatment effect. In the following I will refer to the condition that starts with the Borrowing treatment as Borrowing First (BF) and to the condition that starts with the Saving treatment as Saving First (SF).

Note that the CARA utility function used in this experiment is defined on the negative domain. In fact, negative consumption was and had to be possible in order to enforce borrowing. However, the experimental environment was designed in such a way that negative consumption was never part of the optimal solution. The fact that out of 9120 consumption decisions only 24 or 0.3% were negative, illustrates that this was generally understood by the subjects. How negative consumption was explained to subjects is part of the next subsection.

### 2.1 Experimental Procedures

Before the start of the experiment, subjects were given time to read the instructions. The experimenter then read the instructions aloud. After this, subject were asked to

\(^8\)Subjects did not know about the role change when playing the first three repetitions. They received new instructions after the third round.
answer a quiz on the contents of the instructions. The correct answers were then read aloud, in order to make sure that everyone understood the instructions.9

Consumption was explained to the subjects as buying “points” by spending “Taler”, the experimental currency in which income was denoted. Experimental currency was converted to points by the utility function specified above. Subjects were informed about the exact form of the utility function. Furthermore they were given a graph of the function and a table with relevant function values. The advantage of framing consumption as buying points is that negative consumption can be explained as the selling of points in return for experimental currency.

Consumption decisions were input in an interface that displayed period income, savings from the last period along with the history of all previous decisions and relevant values, such as savings, wealth, the number of purchased points, and accumulated points. Before a consumption decision was implemented, subjects were informed about how their chosen consumption level translates into points and the amount of savings that would be available in the next period. After this information was displayed subjects had the opportunity to start over, i.e. specify another potential level of consumption, and check the implications of that consumption level. In the final period of each life cycle, the program automatically spent that period’s wealth as consumption. Then subjects were informed about the amount of points they purchased during the round on a separate screen. At the end of the experiment, two of the six experimental life cycles were randomly chosen to be payoff relevant, one from the first three life cycles and one from the last three life cycles. Subjects’ payoffs were determined by a preannounced linear function of the amount of points purchased in the two relevant rounds. The minimal payoff was fixed at 5 €. Subjects earned an average of 19.23 €.

The experiment was conducted at the laboratory of the Berlin University of Technology. The experiment was programmed and conducted with the software z-Tree (fischbacher2007). A total of 76 subjects participated, 38 in the Borrowing First condition and 38 in the Saving First condition. Most of the subjects were undergraduate students in the field of economics or engineering.

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9See Appendix B for the instructions and the quiz
Figure 1: Mean and median consumption over all subjects in the Borrowing First and Saving First conditions.
3 Results

Figure 1 shows mean and median consumption for each period of the experiment, separated by the BF and SF condition. Optimal consumption is indicated by a solid grey line. Whenever subjects face an increasing income stream, i.e. in rounds one to three in the BF condition and in rounds four to six in the SF condition, mean and median consumption appears to be increasing within rounds. Whenever subjects face a decreasing income stream (rounds four to six in the BF condition and rounds one to three in the SF condition) mean consumption appears do be declining within rounds. Median consumption appears to be relatively close to optimal consumption. Overall this first glance at the data suggests that subjects deviate systematically from optimal consumption. In particular, consumption appears to follow income to some extend, and deviations appear to be higher in the Borrowing treatment than in the Saving treatment.

Deviations from optimal consumption will be analyzed in more detail in subsection 3.1. In subsection 3.2, I will discuss the theoretical implications of myopia in this experiment and estimate subjects’ apparent planning horizons. In subsection 3.3, I will examine learning effects, i.e. whether subjects improve their decisionmaking over the 6 experimental life cycles.

3.1 Deviations from Optimal Behavior

There are two ways to measure deviations from optimal behavior. Actual consumption levels can be compared to consumption levels that would be optimal, given a subject has always behaved optimally in the past, i.e. has optimal wealth levels in any period. I will refer to this consumption level as unconditionally optimal consumption. Another way is to compare actual consumption levels to the consumption level that would be optimal given the actual wealth levels that subjects have at the considered period of the experiment. I will refer to this consumption level as conditionally optimal consumption. Like carbone2004 I will make use of both concepts, however I prefer the latter one for the following reason: an error made in one period causes the wealth level in the following period to deviate from the unconditionally optimal level. Since optimal consumption is a function of present wealth, optimal consumption in the next period will also deviate from unconditional optimal consumption. An optimal response to the present wealth level in the next period would thus be counted as a deviation from unconditionally op-
timal behavior. Furthermore, an error made in any period causes optimal consumption to deviate from unconditionally optimal levels in all following periods, even if a subject behaved optimally from that period onwards. Comparing actual consumption levels to unconditionally optimal levels therefore results in a multiple counting of one error and thus leads to a disproportionate weighting of early errors compared to later errors.

I will start by analyzing directional deviations from optimal consumption, i.e. whether subjects consume too much or too little compared to optimal consumption.\(^{10}\) A measure for directional deviations from optimal consumption used by Ballinger 2003 is given by Measure 1: \( m_1 = \sum_{t=1}^{20} (c^*_t(w_t) - c_t) \), where \( c^*_t(w_t) \) is conditionally optimal consumption (depending on current wealth \( w_t \)) and \( c_t \) is observed consumption in period \( t \). This is the sum of deviations from conditionally optimal consumption for one subject and over one experimental life-cycle. For the sake of legibility I omit indices for subjects and rounds. Figure 2 provides a graphical representation of the median measure \( m_1 \) of all subjects from the BF condition (solid line) and the SF condition (dashed line) for rounds 1 to 6.\(^{11}\) The grey error bars represent the 95% confidence intervals (from a Wilcoxon signed-rank test).

Whenever subjects faced an increasing income stream, i.e. in round 1 to 3 in the BF condition, as well as in round 4 to 6 in the SF condition, \( m_1 \) is significantly positive. This implies that subjects on average consume less than optimal in each of these rounds. Note that this result is contrary to previous experimental studies, where subjects are found to typically consume too much relative to optimal levels. A potential explanation is that with an increasing income stream, borrowing is necessary for optimal consumption. Since previous experimental studies did not allow borrowing, their findings might not hold for borrowing behavior. The evidence is not as clear concerning deviations from optimality when subjects face a decreasing income stream, i.e. in round 1 to 3 in the SF condition and in round 4 to 6 in the BF condition. All median \( m_1 \) values are negative, however only three of them significantly so. This implies that subjects (weakly) overconsume relative to optimal levels, which is in line with previous findings.

The measure introduced above gives account of whether subjects mostly consume more or less than is optimal throughout one experimental life-cycle. However, it is not a very good measure of performance, since it potentially conceals suboptimal behavior.

\(^{10}\)Note that consumption and savings are two sides of one coin: a subject who consumes too little also saves too much and vice versa.

\(^{11}\)I use the median as a descriptive statistic because I use non-parametric tests, such as the Mann-Whitney U Test to compare treatments. These tests typically provide information about the median of a random sample.
This is the case, for instance, when positive and negative deviations cancel each other out over one experimental life-cycle. Even though the median deviation is close to zero, as observed in rounds 1 to 3 in the SF condition, behavior might still be far from optimal. Therefore I also examine absolute deviations from conditional optimal behavior by use of Measure 2, \( m_2 = \sum_{t=1}^{20} |c^*_t(w_t) - c_t| \). Figure 3(a) illustrates the evolution of Measure 2 over the six experimental life-cycles. Again, the solid line represents the median \( m_2 \) over all subjects in the BF condition and the dashed line represents the median \( m_2 \) over all subjects in the SF condition. The median levels of \( m_2 \) are higher when subjects face an increasing income stream than when they face a decreasing income stream. This relationship is significant for the first three rounds (p-values from a Mann-Whitney U test are provided in Table 1). This suggests that absolute deviations from conditionally optimal behavior are higher when subjects have to borrow in order to consume optimally than when they have to save in order to consume optimally.

As discussed in Section 2, all subjects observe the same income shock realizations  

\[ \text{Figure 2: Median aggregate deviation from conditional optimal consumption. Solid and dashed lines represent median values from the BF and SF condition respectively.} \]
Table 1: Mean and median measures 1-3 and apparent planning horizon $h^*$, separated by conditions and rounds. P-values are calculated by use of Mann-Whitney U tests and are printed in italic letters. The null hypothesis is that samples are stochastically equivalent.
Figure 3: Median aggregate absolute deviations from conditionally optimal consumption and median utility loss. Solid and dashed lines represent median values from the BF and SF condition respectively.

over the course of the experiment. Furthermore subjects from both the BF and SF condition share the same unconditional optimal consumption levels at any period and round during the experiment. Therefore I can directly compare deviations from unconditional optimal behavior across treatments. Measure 3 is \[ m_3 = \sum_{t=1}^{20} (u(c^*_t(w^*_t)) - u(c_t)) \]

where \( c^*_t(w^*_t) \) denotes unconditionally optimal consumption at period \( t \) as a function of optimal wealth \( w^*_t \). This measure can be interpreted as the utility loss that results from suboptimal consumption in one experimental life-cycle. Using conditionally optimal consumption utility as a benchmark yields similar results, however the interpretation is not as straightforward. Figure 3(b) summarizes the median utility loss for the BF and SF conditions. Similar to the previous results, utility loss is higher for subjects in the Borrowing treatments compared to subjects in the Saving treatments. This difference is significant in rounds one and three and marginally significant (p=0.059) in round two.\footnote{Subjects may perceive the role change after round three to reveal new information about the structure and purpose of the experiment, which may lead them to reconsider their strategy. Therefore, the fact that the differences in \( m_2 \) and \( m_3 \) seize to be significant after the role change is not overly surprising.}

\[ \text{be zero, since } \sum_{t=1}^{20} c^*_t(w^*_t) = \sum_{t=1}^{20} c_t, \text{ where } c^*_t(w^*_t) \text{ denotes unconditionally optimal consumption at period } t \text{ as a function of optimal wealth } w^*_t, \text{ always holds.} \]
Summing up, the data suggest that there are substantial deviations from optimal behavior. In particular, subjects consume less than optimal when they face an increasing income stream. Only weak evidence exists for overconsumption when the income stream is decreasing. There appears to be a difference in deviations between the Borrowing and Saving treatments. Deviations from optimal consumption are higher in the Borrowing treatment than in the Saving treatment. This implies that subjects are less willing to borrow than they are willing to save in order to smooth consumption, i.e. they are debt averse.

3.2 Myopia

Some authors suggest that sub-optimal consumption choices can be explained with myopia, a particular form of bounded rationality. In order to behave optimally in this experiment, subjects have to solve a backward induction problem that has 20 induction steps. Since this is a very complex problem it comes as no surprise that subjects fail to behave optimally. Ballinger et al. (2003) suggest that subjects may have a limited ability to plan ahead, i.e. their planning horizon may be shorter than the experimental time horizon. In this experiment, the short-horizon (myopic) optimal solution generally deviates from the full horizon optimal solution, unless the remaining periods are less or equal the planning horizon.

Myopia is an appealing model of behavior since it can not only explain deviations from optimal behavior, but in this experimental environment also makes clear predictions concerning the direction of deviations from optimal behavior. Myopic subjects are expected to over-consume in the Saving treatment and to under-consume in the Borrowing treatment. In the Saving treatment, a shorter planning horizon implies that subjects do not take later periods into account, where income is lower. Hence they underestimate the need to save for later periods and consume more than is optimal. Analogously, in the Borrowing treatment a shorter planning horizon implies that later, higher income periods are neglected. Hence, myopic individuals do not borrow enough and therefore consume less than is optimal. These predictions appear to be in line with the findings from subsection 3.1, where significant underconsumption is observed in the Borrowing treatment and weak evidence is found for overconsumption in the Saving treatment.

Myopia can furthermore explain certain differences in deviations from conditional optimal behavior between the Borrowing and the Saving treatment. In particular,
when a positive income shock occurs, the absolute deviation from (full horizon) optimal behavior of a myopic agent will be higher in the Borrowing treatment than in the Saving treatment. Vice versa, when a negative income shock occurs, the deviation is higher in the Saving treatment than in the Borrowing treatment. One of the main results from subsection 3.1 is that deviations from optimal behavior are higher for subjects in the Borrowing treatment than for subjects in the Saving treatment. It therefore seems necessary to examine whether this result can be explained by myopia. To address this issue I estimate the subjects’ apparent planning horizons and check whether planning horizons are consistent across treatments. The apparent planning horizon is estimated as:

$$h^* = \arg\min_{h \in \{1, \ldots, 20\}} \sum_{t=1}^{20} (c_t^M(w_t, h) - c_t)^2,$$

where $c_t^M(w_t, h)$ is conditional optimal (myopic) consumption given the planning

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The appendix contains an example that illustrates how myopia affects deviations from full horizon optimal behavior.
The adopted approach of estimating the planning horizon is identical to that of ballinger2003 and has since been used repeatedly in the literature on life-cycle consumption experiments. Figure 4 illustrates the median estimated planning horizons. Estimated planning horizons are lower for subjects in the Borrowing treatment compared to subjects in the Saving treatment. This difference is significant at the 5% level for all rounds. This result is interesting since there exists no a-priori reason for subjects to have different planning horizons in the different treatments.

If Myopia was the only explanation for the observed deviations from optimality, this explanation should be independent of the treatment, and one should therefore observe planning horizons that are similar across treatments. This is clearly not the case.

Summing up, while myopia can explain certain characteristics of the experimental data, it fails to consistently explain observed behavior in this experiment. There is no a-priori reason why planning horizons should differ across treatments, since subjects are randomly assigned to treatments. This suggests that some other factor, not captured by the concept of myopia (e.g. debt aversion) drives behavior and causes the difference in estimated planning horizons.

3.3 Learning

In order to assess whether subjects are able to improve their consumption decisions over time, I look at within subject differences in the absolute deviations from conditional optimal consumption (Measure 2) across rounds. Table 2 summarizes the median differences in measure $m_2$ between consecutive rounds as well as to the first round. The difference between round $r$ and the first round is denoted by $\Delta_1^r m_2 = m_2^1 - m_2^r$ and the difference between two consecutive rounds is denoted by $\Delta_{r-1}^r m_2 = m_2^{r-1} - m_2^r$. There appears to be a constant improvement of consumption decisions in the BF condition. All median differences between two consecutive rounds are positive and most of these differences are significant. Moreover, all rounds show significant improvement in comparison to the first round. One has to be careful, however, when comparing data from two different treatments, i.e. data from the first three rounds and data from the second three rounds. Differences in behavior can be caused by both learning and the treatment

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$^{15}$I also estimated $h^*$ using absolute deviations instead of squared deviations. The results are almost identical.

$^{16}$see, for instance, carbone2004 ballinger2011

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16
Table 2: Median differences in $m_2$ between consecutive rounds and to the first round. P-values are printed in italic letters and are calculated by use of Wilcoxon signed-rank tests. The null hypothesis is that the median difference between the pairs is zero.

<table>
<thead>
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<th>measure</th>
<th>condition</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
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<tr>
<td>$\Delta_{r-1}m_2$</td>
<td>BF</td>
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<td>98.323</td>
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<tr>
<td>$\Delta_{r-1}m_2$</td>
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<td>$&lt;0.001$</td>
<td>0.408</td>
<td>0.750</td>
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</table>

The significant improvement of consumption decisions between round 3 and 4 is therefore probably caused by a combination of learning and the treatment effect. In the SF condition, consumption decisions improve from round 1 to 2 and from round 2 to 3 before they significantly deteriorate between rounds 3 and 4. After round 3 the differences to the first round are not significantly different from zero, implying no improvement in comparison to the first period. Again both learning and treatment effect play a role here. Generally one would expect the learning effect to positively influence consumption decisions. However, the overall effect between rounds 3 and 4 is significantly negative. This implies that the treatment effect is negative and that it dominates the learning effect.

Note that when comparing rounds 3 and 4, the within subject effect is the same as in the between subject analysis in Section 3.1. When changing from the Borrowing to the Saving treatment there is an improvement of consumption decisions (even though here it is not possible to discriminate between the learning and the treatment effect). The treatment effect here is the change of the income process, which determines whether saving or borrowing is necessary for optimal consumption.
and when changing from the Saving to Borrowing treatment consumption decisions deteriorate.

Comparing learning rates (i.e. $\Delta r^{-1}m_2$) between the two conditions allows to identify potential differences in learning across the two conditions. No significant difference in learning rates between BF and SF is found in any round, except round 4: $\Delta^3 m_2$ is significantly higher in the BF condition compared to the SF condition (Mann-Whitney U test, p-value < 0.001). However, as stated above, between round 3 and 4, both learning and the treatment effect are present, and therefore the difference in $\Delta^3 m_2$ between the two conditions is likely caused by the treatment effect.\(^\text{18}\)

Overall these findings imply that subjects generally learn and improve their consumption decisions over time. However, experience does not seem to eliminate the treatment effect. Even after three rounds of learning in the Saving First condition, consumption decisions markedly deteriorate when subjects have to borrow in order to consume optimally. In other words: the finding that subjects perform worse when they have to borrow in order to consume optimally compared to when they have to save in order to consume optimally, prevails even after subjects learn to improve their decisionmaking, i.e. learn to smooth consumption.

\section*{4 Discussion and Conclusion}

With the experiment presented in this paper I am able to assess saving behavior as well as borrowing behavior in a dynamic optimization context. Previous experiments on life-cycle consumption problems done by others find a general tendency for subjects to save too little. This study suggests that this result does not hold when borrowing is allowed and necessary for optimal consumption. In this experiment, the direction of deviations from optimal behavior is context specific. There exists weak evidence that subjects save too little and consume too much (relative to conditionally optimal consumption) when the income stream is decreasing and saving is necessary for optimal consumption. Subjects borrow too little and thus consume too little when the income

\[^{18}\text{Figure 3 appears to suggest that there are different learning rates in the two treatments, since the median } m_2 \text{ is declining in the saving treatment and somewhat constant in the borrowing treatment. With respect to learning, this figure may be misleading because the median of (within subject) differences between two rounds is not necessarily the same as the difference between the medians of two rounds, i.e.: median($m_2^{-1} - m_2^j$) $\preceq$ median($m_2^{-1}$) - median($m_2^j$). The right hand side of this inequality is presented in Figure 3 and Table 1, and the left hand side in Table 2. In order to analyze learning effects, I am focusing on within subject differences between rounds, i.e the left hand side of the above inequality.}\]
stream is increasing and borrowing is necessary for optimal consumption. Furthermore, the experimental data suggest that deviations from optimal behavior are higher when subjects have to borrow than when they have to save in order to reach optimal consumption. This implies that subjects are less willing to engage in debt than in savings, i.e. they are debt averse. Similar to other experiments on intertemporal consumption/savings problems, learning is observed here. However, subjects seem to be unable to transfer what they have learned in the Saving treatment to the Borrowing treatment. In fact, consumption decisions significantly deteriorate after the role change from the Saving to the Borrowing treatment, suggesting that the effect that debt aversion has on consumption decisions prevails even after three rounds of experience.

Often stated reasons in the literature for sub-optimal consumption choices are bounded rationality, in particular limited planning horizons (or myopia), as well as time-inconsistent preferences. Myopia is an appealing model of behavior, because it can explain overconsumption with a decreasing income stream and underconsumption with an increasing income stream. However, myopia cannot explain the asymmetry between deviations from optimal consumption with an increasing and with a decreasing income stream. This intuition is confirmed by the fact that significantly different apparent planning horizons are estimated in the different treatments. Since one would expect planning horizons to be equally distributed in both treatments, this implies that myopia alone cannot explain the observed differences in behavior. Other forms of computational constraints, e.g. “cost of thinking”, may explain deviations from optimal behavior but not the difference in behavior across treatments. This is because the difficulty of the optimization problem is the same in both treatments, as debt is mathematically equivalent to savings, only with a different sign.

Present biased preferences cannot serve as an explanation for the deviations from optimality either. Subjects in this experiment receive their (monetary) reward at only one point in time, which is after the experiment. It seems unlikely that some form of present bias affects consumption decisions during the experiment since there exist no immediate rewards. Brown2009 use sips of water as immediate rewards for thirsty subjects to emulate an intertemporal consumption/savings environment where present biased preferences can play a role. A simple $\beta - \delta$ model of discounting would predict that agents facing an increasing income stream borrow too much, which is opposite to the findings in this paper. Therefore, analyzing behavior in an environment where both debt aversion and present bias are relevant, appears to be a promising future research project.
Another reason that might explain the observed asymmetry in behavior across the two treatments is lack of experience with borrowing, as one could argue that the participants of this experiment (mostly undergraduate students) do not have much borrowing experience. Hence, the observed difference could reflect the fact that subjects simply do what they are used to, i.e. to save but not to borrow in order to smooth consumption. More research is needed to explore the interaction of debt aversion and borrowing experience. However, I believe it is safe to say that at least in the domain of the small experimental stakes, subjects do have sufficient borrowing experience (e.g. borrowing 10€ from friends or family).

\footnote{In particular, it is hard to identify causality. Abstaining from debt could be due to lack of borrowing experience as well as debt aversion. Lack of borrowing experience, however, could also be caused by debt aversion.}
Appendix

A Myopia and deviations from optimal behavior

Example 1: Assume we are in the first period of the 20-period life-cycle consumption environment described in Section 2. Further assume that the decisionmaker is myopic and has a planning horizon of 2, that is when making a decision she acts as if the the next period is the final period. Myopic optimal consumption $c^M$ in period 1 follows from the two-period optimization problem:

$$c^M = \arg \max_{c_1} [u(c_1) + u(y_1 - c_1 + E[y_2])]$$

(8)

As explained in Section 3, different optimal myopic consumption levels arise in the different treatments. Since optimal consumption is a function of period wealth, optimal consumption levels also depend on the income shock. Long-term (fully rational) optimal consumption only depends on the income shock and does not differ between treatments.

1. **Borrowing treatment (increasing income stream):** Short-term (myopic) optimal consumption is:

$$c_B^M = \begin{cases} 9.503 & \text{if } y_1 = 0 \text{ (negative income shock)} \\ 19.503 & \text{if } y_1 = 20 \text{ (positive income shock)} \end{cases}$$

(9)

2. **Saving treatment (decreasing income stream):** Short-term (myopic) optimal consumption is:

$$c_S^M = \begin{cases} 189.503 & \text{if } y_1 = 190 \text{ (negative income shock)} \\ 199.503 & \text{if } y_1 = 210 \text{ (positive income shock)} \end{cases}$$

(10)

Long-term optimal consumption does not differ between treatments and is given by:

$$c^L = \begin{cases} 104.322 & \text{with negative income shock} \\ 105.322 & \text{with positive income shock} \end{cases}$$

(11)

It is straight-forward to see that deviations from long-term optimal behavior caused by myopia are higher in the Borrowing treatment than in the Saving treatment when
an negative income shock occurs:

\[ \Delta_{B}^{neg} = 104.322 - 9.503 = 94.819 > \Delta_{S}^{neg} = 189.503 - 104.322 = 85.181. \quad (12) \]

Analogously, with a positive income shock deviations in the Saving treatment are higher than in the Borrowing treatment:

\[ \Delta_{B}^{pos} = 105.322 - 19.503 = 85.819 < \Delta_{S}^{pos} = 199.503 - 105.322 = 94.181. \quad (13) \]

\section*{B Instructions}

This section contains the instructions of the experiment.\textsuperscript{20} The first part of the instructions were given to subjects in a printed handout and were read aloud by the experimenter. After this, subjects were asked to complete a quiz on the content of the instructions. The correct answers to the questions of the quiz were then also read aloud. The second part was handed out to subjects when they finished the third round. Subjects in the different conditions received different instructions. The instructions printed here were used for subjects from the Borrowing First condition.

\textbf{Instructions (Part 1)}

The experiment you are participating today is part of a research project. It is meant to analyze economic decision making. The rules and instructions are the same for every participant. Your payoff depends on your decisions during the experiment. Please read the instructions carefully. You are not allowed to talk and exchange information with other participants during the experiment. Please raise your hand if you have a question. An Experimenter will then come to your place and answer your question. Please don’t ask your questions out loud. Should you break one of these rules we are obliged to exclude you from participation.

\textbf{Overview.} First you will have time to read the instructions. After that we will go through the instructions together and you answer a quiz in order to make sure you

\textsuperscript{20}The instructions printed here are a translation of the original German version.
understood the instructions. After that you may ask questions, before the experiment starts. After the experiment you will be asked to fill out a short questionnaire.

The experiment consists of 6 rounds, each of which consists of 20 periods. The duration of the experiment is around 1.5 hours. Instructions, quiz and questionnaire will take around 30 minutes. The remaining hour is dedicated to the actual experiment. In every period a countdown of 30 seconds will be displayed. You may take more or less time to reach your decision. The countdown is meant to provide some indication how much time you can take in every period to finish the experiment in one hour. You may finish the experiment even if you play for more than one hour.

The following instructions are for the first three rounds of the experiment. After three rounds the experiment stops and you will be asked to type in a password. You will be handed new instructions for the following 3 rounds, containing the password needed to continue with the experiment. After the last round your experiment payoff will be displayed. Please raise you hand when you have finished the last period. You will then be handed a short survey. After filling out the survey, please raise your hand again. You will then be given your experiment payoff.

You are playing an “investment game” and decide in every period how many points you want to purchase. The sum of all points purchased in one round is that period’s result. Your payoff depends the results from two randomly drawn rounds.

**Income, Savings and Wealth.** In every period you obtain a certain income, denoted in the experimental currency “Taler”. Your task is to choose how many taler to spend in order to purchase points. Thereby you (implicitly) also choose how many Taler you want to save or borrow. The difference between income and spending in one period are called savings. At any period in the experiment, your wealth is defined as the sum of savings from all previous periods. This implies that savings from one period added to the wealth in this period yields the wealth in next period. Please note that the sign of the savings can be both positive and negative. In case you decide to spend less Taler than you have as income, your savings have a positive sign. In this case your wealth in the next period is your waltz in this period plus the absolute amount of savings in this period. Should you decide to spend more Taler than you have as income, your savings have a negative sign. In this case your wealth in the next period is your wealth in this period minus the absolute amount of savings.
Example: assume your income in one period is 50 Taler and you spend 30 Taler to purchase points. Your savings are then 20 Taler. In case you instead spend 70 Taler with the same income, your savings are -20 Taler. In the first case your wealth in the next period is the wealth in this period plus 20 Taler. In the latter case your wealth in the next period is this period’s wealth minus 20 Taler.

Your wealth may take positive or negative values as well, depending on whether your savings from previous periods were positive or negative. Your wealth in the first period is 0 Taler. In the last period, your wealth plus income will be spent automatically in order to purchase points. This implies that the sum of Taler spent in all periods of one round equals the sum of income obtained in all periods of this round. In other words: you may spend more or less than your income in one round. However, over one round, the sum of income always equals the sum of Taler spent.

**Determination of Income.** Income is randomly determined and follows the random process:

\[ y_t = 10t + \epsilon_t \]

The index “t” denotes the periods for which income is determined. Since the slope of the process is 10, it has a positive trend. The expected income is therefore increasing over time. \( \epsilon_t \) is the random part of the process and can be either +10 or -10, both occurring with equal probability of 50%. Since \( \epsilon_6 \) is either +10 or -10, your income in period 6 is either 70 or 50. Since one round consists of 20 periods, income in the last period will either be 210 or 190. It is very important to understand that \( \epsilon_t \) is truly randomly determined. Which value \( \epsilon_t \) takes in one period does not depend on which values it had in previous periods or how you behaved in previous periods.

**Taler and Points.** Your task to decide in every period how many Taler you want to spend in order to purchase points. Taler are transformed to points as follows:

\[ \text{Points} = 250(1 - e^{-0.02 \times \text{(chosen amount of Taler)}}) \]

A graph of this function, as well as a table with relevant function values is attached to the instructions. Please note that the above function is defined on the positive as well as the negative domain. If you choose to spend a negative amount of Taler, you receive
a negative amount of points. In this case you “sell” points and gain Taler. Should your wealth plus income in the last period be negative, you will have to automatically sell points in order to make sure that your Taler account is balanced.

**Payoff.** Your payoff depends on the results from two randomly drawn rounds. One round is randomly drawn from the first three rounds and the other is randomly drawn from the second three rounds. Your payoff is calculated as follows:

\[
\text{Payoff in Euro} = \frac{(\text{Result1} - 3000) + (\text{Result2} - 3000)}{100}
\]

where Result1 is the first randomly drawn result and Result2 is the second randomly drawn result.

**Example:** suppose the first randomly drawn result is 4300 points and the second randomly drawn result is 3800 points. Your payoff is then:

\[
\frac{(4300 - 3000) + (3800 - 3000)}{100} = \frac{1300 + 800}{100} = 21 \text{ €}.
\]

**Quiz and Questions.** You will now be asked to answer a short Quiz regarding the contents of these instructions. In case you have questions after that, please raise your hand. An experimenter will then come to you and answer your question.
Instructions (Part 2)

In the following three rounds the random process that determines your income will change. Therefore, compared to the first part of the instructions, only the paragraph “Determination of Income” changes. The rest of the instructions is still valid.

**Determination of Income.** Income is randomly determined and follows the random process:

\[ y_t = 210t - \epsilon_t \]

The index “t” denotes the periods for which income is determined. Since the slope of the process is -10, it has a negative trend. The expected income is therefore decreasing over time. \( \epsilon_t \) is the random part of the process and can be either +10 or -10, both occurring with equal probability of 50%. Since \( \epsilon_6 \) is either +10 or -10, your income in period 6 is either 140 or 160. Since one round consists of 20 periods, income in the last period will either be 20 or 0. It is very important to understand that \( \epsilon_t \) is truly randomly determined. Which value \( \epsilon_t \) takes in one period does not depend on which values it had in previous periods or how you behaved in previous periods.
Figure 5: Graph of the Utility Function

Figure 6: Table with relevant function values
Quiz

Income

a) True or false: your income in period 7 is either 70 or 80.
   Your answer: Correct answer:

b) True or false: your income in period 19 is either 180 or 200.
   Your answer: Correct answer:

c) What is the probability of your income to be 180 Taler in period 19?
   Your answer: Correct answer:

d) Suppose you were “lucky” in period 10, and received 110 Taler. How high is the probability to be lucky in the next period and receive 120 Taler?
   Your answer: Correct answer:

Wealth and Savings

Suppose your wealth in some period is 100 Taler. Your income is 60 Taler. You decide to spend 55 Taler to purchase points.

a) What is the amount you save this period?
   Your answer: Correct answer:

b) What will be our wealth in the next period?
   Your answer: Correct answer:

Suppose you decide instead to spend 70 Taler.

c) What is the amount you save this period?
   Your answer: Correct answer:

d) What will be your wealth in the next period?
   Your answer: Correct answer:
Points and Taler

a) Have a look at the enclosed table. Suppose you wish to spend 300 Taler. How many points will you receive?

Your answer: Correct answer:

b) Suppose you want to spend -10 Taler. How many Taler do you get in return?

Your answer: Correct answer:

c) Suppose you want to buy 45.32 points. How many Taler do you have to spend?

Your answer: Correct answer:

d) Suppose you want to buy 247.49 points. How many Taler do you have to spend?

Your answer: Correct answer:

d) Suppose you want to “sell” 122.96 Taler (i.e. buy -122.96 points). How many Taler do you get in return?

Your answer: Correct answer:

Your Payoff

Suppose your period earnings in rounds 1 to 6 are: 3100, 5000, 4300, 3500, 3700 and 4000 points respectively.

a) The random draw determines rounds 1 and 5 to be payoff relevant. How many Euro do you earn?

Your answer: Correct answer:

b) The random draw determines rounds 3 and 4 to be payoff relevant. How many Euro do you earn?

Your answer: Correct answer: